

TRANSFORMADA DE LAPLACE E PROPRIEDADES

Transformada de Laplace de $f(t)$: $L[f(t)] = F(s) = \int_0^\infty e^{-st} f(t) dt$

Transformada inversa de Laplace de $F(s)$: $L^{-1}[F(s)] = f(t)$ se $L[f(t)] = F(s) = \int_0^\infty e^{-st} f(t) dt$

	Transformada	Transformada inversa
1	$L[\delta(t-a)] = e^{-as}$	$L^{-1}[e^{-as}] = \delta(t-a)$
2	$L[u(t-a)] = \frac{e^{-as}}{s}$	$L^{-1}\left[\frac{e^{-as}}{s}\right] = u(t-a)$
3	$L[e^{at}] = \frac{1}{s-a}$	$L^{-1}\left[\frac{1}{s-a}\right] = e^{at}$
4	$L[\cos(at)] = \frac{s}{s^2 + a^2}$	$L^{-1}\left[\frac{s}{s^2 + a^2}\right] = \cos(at)$
5	$L[\sin(at)] = \frac{a}{s^2 + a^2}$	$L^{-1}\left[\frac{a}{s^2 + a^2}\right] = \sin(at)$
6	$L[\cosh(at)] = \frac{s}{s^2 - a^2}$	$L^{-1}\left[\frac{s}{s^2 - a^2}\right] = \cosh(at)$
7	$L[\operatorname{senh}(at)] = \frac{a}{s^2 - a^2}$	$L^{-1}\left[\frac{a}{s^2 - a^2}\right] = \operatorname{senh}(at)$
8	$L[t^n] = \frac{n!}{s^{n+1}}, n = 1, 2, 3, \dots$	$L^{-1}\left[\frac{1}{s^{n+1}}\right] = \frac{1}{n!}t^n, n = 1, 2, 3, \dots$
9	$L[t^n \cdot e^{at}] = \frac{n!}{(s-a)^{n+1}}, n = 1, 2, 3, \dots$	$L^{-1}\left[\frac{1}{(s-a)^{n+1}}\right] = \frac{1}{n!}t^n \cdot e^{at},$
10	$L[e^{at} \cos(bt)] = \frac{s-a}{(s-a)^2 + b^2}$	$L^{-1}\left[\frac{s-a}{(s-a)^2 + b^2}\right] = e^{at} \cos(bt)$
11	$L[e^{at} \sin(bt)] = \frac{b}{(s-a)^2 + b^2}$	$L^{-1}\left[\frac{b}{(s-a)^2 + b^2}\right] = e^{at} \sin(bt)$
12	$L[e^{at} f(t)] = F(s-a)$	$L^{-1}[F(s-a)] = e^{at} L^{-1}[F(s)]$
13	$L[f'(t)] = sL[f(t)] - f(0)$	
14	$L[f^{(n)}(t)] = s^n L[f(t)] - s^{n-1}f(0) - \dots - f^{(n-1)}(0)$	
15	$L\left[\int_0^t f(\tau) d\tau\right] = \frac{1}{s} L[f(t)]$	$L^{-1}\left[\frac{1}{s} F(s)\right] = \int_0^t L^{-1}[F(s)](\tau) d\tau$
16	$L\left[t^n \cdot f(t)\right] = (-1)^n \frac{d^n}{ds^n} L[f(t)]$	$L^{-1}\left[\frac{d^n}{ds^n} F(s)\right] = (-1)^n t^n \cdot L^{-1}[F(s)]$
17	$L[u(t-a) \cdot f(t-a)] = e^{-as} L[f(t)]$	$L^{-1}[e^{-as} F(s)] = u(t-a) \cdot f(t-a)$
18	$L[u(t-a) \cdot f(t)] = e^{-as} L[f(t+a)]$	
19	$L\left[\int_0^t f(t-v) g(v) dv\right] = F(s) \cdot G(s)$	$L^{-1}[F(s) \cdot G(s)] = \int_0^t f(t-v) g(v) dv$
20	$L\left[\frac{f(t)}{t}\right] = \int_s^{+\infty} L[f(t)](v) dv, \text{ se } \lim_{t \rightarrow 0} \frac{f(t)}{t} \text{ finito}$	$L^{-1}\left[\int_s^{+\infty} F(v) dv\right] = \frac{1}{t} L^{-1}[F(s)]$